

Operator precedence cheat sheet for Isabelle/HOL (quick and dirty, little quality control, version 2012-Nov-12). Follow-up of the discussion at the Isabelle mailing list in November 2012, <https://lists.cam.ac.uk/pipermail/cl-isabelle-users/2012-November/msg00020.html>. Entries without a fixed precedence are still rough guesstimates (that may need further correction).

| Class | Precedence | Symbols and the minimum precedence of symbols that may be contained in non-terminals |
|------------|------------|--|
| function | | application of user-defined function, field dereference (record) |
| function | 900 | (900 \langle 0 \rangle (record update)) |
| function | 100 | (100 nth (list) 101) |
| type | | “set” type constructor, “list” type constructor |
| function | 70 | (70 \cap (set) 71), (70 * (nat) 71) |
| function | 65 | (65 \cup (set) 66), (65 + (nat) 66), (65 - (nat) 66), (66 # (list) 65), (66 @ (list) 65) |
| relation | 50 | (50 = 51), (50 \in 51), (51 < 51), (51 \leq 51) |
| logic | 40 | (\neg 40) |
| logic | 35 | (36 \wedge 35) |
| logic | 30 | (31 \vee 30) |
| logic | 25 | (26 \longrightarrow 25), (26 \leftrightarrow 25) |
| logic | 10 | (\forall 0 . 10), (\exists 0 . 10), (if 0 then 0 else 10), (case 0 of 10), (let 0 in 10) |
| type | 3 | (4 :: 0) |
| logic | 3 | (λ 0 . 3) |
| metallogic | 2 | (3 \equiv 2) |
| metallogic | 1 | (2 \implies 1) |
| type | 0 | (1 \Rightarrow 0) |
| metallogic | 0 | (\bigwedge 0 . 0) |

Table 1: Higher symbols have higher precedence. Precedences given where known to me, by use of the Isabelle command “print_syntax” - you can issue this command for example anywhere in an empty theory or an existing theory. “print_syntax” also shows precedence for a lot of symbols not given in the table for brevity (say, exponentiation of natural numbers). Following the convention of the output of “print_syntax”, associativity of binary operators is determined by that a non-terminal in the right-hand side production rule of a grammar only may be expanded by non-terminals with the same or higher precedence. Hence, for example addition on the natural numbers is left-associative, as its production still allows expansion to the left of the “+” operator. Conversely, for example list concatenation is right-associative. “<” is not associative at all (no expansion allowed either way). See also the post by Holger Gast for a more detailed explanation (<https://lists.cam.ac.uk/pipermail/cl-isabelle-users/2012-November/msg00032.html>). Classes are my own interpretation.

Note on classes:

function if it is a function (type constructors “set”, “list” could also be seen as functions)

relation if it is a relation

logic if it is object logic

metallogic if it is meta logic